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Mailly 318- Mailly mathematical Logic

Assignment #7

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## [#] How many functions are there:

(1) from 2 to 3

f: {0,13} -> {0,1123}

141=3

1x1=2

humb of facts = 32=41

Recall: 1-x-y

To be a fact, no elf in

X can have more than one

voilue in Y.

Hence [#o] fact f x=y]=1411111

- (2) from 4 to 2  $f: \{0,1,2,3\} \rightarrow \{0,1\}$  |Y|=2 |X|=Anumber of facts =  $Z^A = 10$
- (3) from 5 to 1

  f: {0,1,2,3,43 -> {0}}

  number of f = 1 (obviously, oill 5 etts will be mappen to 0)
- (4) from 5 to 0
- (5) from 0 to 5

  J. Ø -D {UIII Z13,43

  If we take 5° = 1, there should be 1 fact but this is a bit complex intuitive, it might also be no functions along

## #2 Are the following sets equinumerous?

From class notes

[OII) ~ ZN and & NN

Since ZN P. N. Men. (COII) and (O)

## (2) [0,1] N and [0,∞)

EO,00) NRNZN NZN

⇒ [0,1] N N [0,00] : Equinumerous

## (3) LO, 1] IN and QIN

for QM: This obviously is not a countable set since:

# 2 M < # IN = # QM and ZM is not (ountable)

54 3 00 1

So,  $Z^{IN} \leq IN^{M} \leq (Z^{IN})^{IN}$  Since  $M \leq Z^{IN}$ but  $(Z^{IN})^{IN} = Z^{IN} \times + Z^{IN} \times + Z^{IN}$   $\Rightarrow + IN^{M} = Z^{M}$   $\Rightarrow + IN^{M} = Z^{M}$  $\Rightarrow + IN^{M} = Z^{M}$ 

Therefore, LOIIZINN QM.: equinimerous:

- #3 Which of the following sets are countained before X is countained to its finite of X NIN
  - (1) 7LM Since 2" is concentrable, neither is 72" (2" < 72") Also, argument in #2 (3) applies
  - (a) 723 U 727 7L3 = 7L x 7L x 7L ~ N same for 727. Since both 723 and 727 are by fuct seen in class, so is their union
  - (3) LI 7LL HEIN

As seen in classe, if 72" is countable them (which is the COLLIN SER #3(2)), LI 72" IS OUSO MOUNTAINE Decould be easily proved by 72".

(4) R × Q induction for 72".

IR IS Uniountaine, so IR × Q ~ Z N × N which is not countable.

- How many bindry relation are there on the set {1,2,3}? Since | {1,2,3} = 3 and | {1,2,3} | x | {1,2,3} = 9, There are 29 = 612 relations on {112,3}
- He want all the sets st (1,1), (2,2), (3,3) are include Hence, there are 32-3 other pair we can choose, so 232-3 - 61 sets WI the pairs (1,1) (2,12) (3,3) in then.

#61 How many reflexive and symmetric binary relations?

The relation must contain (1,1), (2,2), (3,3) to be repeated and we also must count the number of relations styles, and  $1 \le i \le j \le n$ ?

=> Z== = Z3 = W , replement a promotive interior

#7 How many eg relation?

According to the theorem of Bell number, it suffices to count the number of partitions to obtain the number of equations.

{ 113, 123, 133} { 213, 123, 133} { 21,23, 133} { 21,33, 123} { 21,23}

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